Examining quantum gravity's effects on gravitational rainbows

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Abstract

This paper delves into the fundamental implications of quantum gravity on gravitational rainbows, an intriguing phenomenon resulting from the interaction between quantum mechanics and gravity. We explore the theoretical underpinnings of quantum gravity and how they affect light bending around enormous objects, providing insight into the phenomenon known as gravitational rainbows. We investigate the complex interplay between quantum gravity and gravitational events by thoroughly analyzing theoretical models, experimental findings, and computer simulations, providing insights into the essence of the cosmos. The results show that according to the basic theories of light propagation, light moves along the x-axis at a constant speed based on observing a straight-line route between the affine parameters and the x-coordinate. The analysis of shifting gravitational potentials reveals significant influences on the routes taken by light beams traveling through gravitational fields. The impact of quantum gravitational effects is emphasized by the gravitational potential spreading outward, reaching magnitudes of $10 \times 10^{11}$ and decreasing towards zero outward. Moreover, the gravitational disturbance distribution is closest to the coordinate system center, with minor perturbations in the z-direction, especially in $h_{xx}$ and $h_{yy}$. This distribution highlights how gravitational influences vary throughout space. Finally, the analysis shows that, due to a decrease in the impact parameter, the deflection angle of light increases as the angle of incidence lowers. Additionally, the deflection angle is directly influenced by the mass of the deflecting objects, suggesting a proportionate link between mass and deflection. These findings advance our knowledge of gravitational events in astrophysical and cosmological contexts and offer insight into how light behaves in gravitational fields.

Keywords: quantum gravity, rainbow, light, quantum, classical mechanics.

Examinando os efeitos da gravidade quântica nos arco-íris gravitacionais

Resumo

Este artigo investiga as implicações fundamentais da gravidade quântica nos arco-íris gravitacionais, um fenômeno intrigante resultante da interação entre a mecânica quântica e a gravidade. Exploramos os fundamentos teóricos da gravidade quântica e como eles afetam a curvatura da luz em torno de objetos enormes, fornecendo informações sobre o fenômeno conhecido como arco-íris gravitacional. Investigamos a complexa interação entre a gravidade quântica e os eventos gravitacionais, analisando minuciosamente modelos teóricos, descobertas experimentais e simulações computacionais, fornecendo insights sobre a essência do cosmos. Os resultados mostram que, de acordo com as teorias básicas de propagação da luz, a luz se move ao longo do eixo x a uma velocidade constante com base na observação de uma rota em linha reta entre os parâmetros afins e a coordenada x. A análise da mudança de potenciais gravitacionais revela influências significativas nas rotas percorridas pelos feixes de luz que viajam através dos campos gravitacionais. O impacto dos efeitos gravitacionais quânticos é enfatizado pelo potencial gravitacional espalhando-se para fora, atingindo magnitudes de $10 \times 10^{11}$ e diminuindo para zero para fora. Além disso, a distribuição da perturbação gravitacional está mais próxima do centro do sistema de coordenadas, com pequenas perturbações na direção z, especialmente em $h_{xx}$ e $h_{yy}$. Esta distribuição destaca como as influências gravitacionais variam no espaço. Finalmente, a análise mostra que, devido a uma diminuição no parâmetro de impacto, o ângulo de deflexão da luz aumenta à medida que o ângulo de incidência diminui. Além disso, o ângulo de deflexão é diretamente influenciado pela massa dos objetos defletores, sugerindo uma ligação proporcional entre massa e deflexão. Estas descobertas avançam o
1. Introduction
Quantum gravity, which aims to reconcile the ideas of quantum mechanics with the gravitational force as defined by Einstein’s general theory of relativity, is one of the most exciting fields of modern theoretical physics. Essentially, quantum gravity aims to elucidate the fundamentals of gravity and spacetime at the lowest scales at which conventional notions of space and time collapse, giving rise to intriguing phenomena and challenging conceptual problems Carlip (2011).

Gravitational rainbows are one such event that has captivated the interest of physicists and astronomers. Due to the strong gravitational fields surrounding huge objects like black holes and neutron stars, light rays passing near them will exhibit distortions in their trajectories known as gravitational rainbows Virbhadra & Ellis, (2000). Colorful rings or arcs are formed due to these distortions; they resemble optical rainbows seen in air rain droplets but on a cosmic scale.

The emergence of gravitational rainbows offers an intriguing opportunity to investigate the regime where quantum gravitational effects become significant, even though the classical theory of general relativity still offers a strong framework for understanding gravity’s behavior in the presence of massive objects Amelino-Camelia et al. (2013). Through examining the departures from classical expectations seen in gravitational rainbows, scientists can learn important things about the structure of spacetime and the quantum basis of gravity at the tiniest possible scales.

We conduct a thorough investigation of the effects of quantum gravity on gravitational rainbows in this paper, covering the theoretical underpinnings, experimental findings, computational simulations, and possible ramifications for our comprehension of the cosmos. Through an interdisciplinary approach that encompasses theoretical physics, astrophysics, and cosmology, we want to illuminate the intricate relationship between quantum mechanics and gravity, gradually revealing the mysteries of the universe gravitationally rainbow by gravitational rainbow.

The general objectives of this work are to review and analyze existing theoretical models of gravitational rainbows in the context of quantum gravity theories, including loop quantum gravity, string theory, and semiclassical approaches.

1.1 Statement of the problem
Gravitational rainbows are an intriguing way to investigate how gravity and quantum mechanics interact. They are caused by gravitational lensing, which bends light near big objects. Although gravitational lensing can be well understood within the context of classical general relativity, the introduction of quantum gravity effects could cause gravitational rainbow production to deviate from conventional expectations. Nevertheless, more research is necessary to fully understand the precise nature and ramifications of these anomalies, which are still poorly understood Amelino-Camelia et al. (2013).

Furthermore, the current theoretical frameworks for gravitational rainbows frequently depend on semiclassical approximations or particular quantum gravity frameworks, such as string theory or loop quantum gravity Carlip (2011). There are still unanswered concerns about these models’ consistency and compatibility with observational data and experimental evidence. Furthermore, because of the intricate nature of the underlying mathematical formalism, the computing tools and techniques needed to mimic gravitational rainbows in the context of quantum gravity theories may present serious difficulties.

Moreover, significant challenges remain in the experimental confirmation and observational identification of quantum gravity effects in gravitational rainbows. Existing observational methods, including astrophysics investigations of neutron stars and black holes, may provide insight into how light behaves in these large objects Virbhadra & Ellis, (2000). However, it is still difficult to identify quantum gravitational signals among the many astrophysical occurrences.

This review intends to methodically examine the most recent theoretical models, computational approaches, and experimental efforts on the effects of quantum gravity on gravitational rainbows in light of these difficulties. This review aims to shed light on the fundamental nature of spacetime and gravity at the quantum level and open
up new research avenues by addressing these open questions and synthesizing current knowledge.

1.2 Significance of the study

This work is significant because it sheds light on the interaction between quantum gravity and gravitational rainbows, which could lead to a deeper understanding of fundamental physics. This work advances our understanding of the fundamental nature of spacetime and gravitational events by examining the effects of quantum gravity theories on the development and characteristics of gravitational rainbows Amelino-Camelia et al. (2013).

There are ramifications for general relativity, quantum mechanics, cosmology, and other fields of physics in comprehending gravitational rainbows within the context of quantum gravity Liberati & Visser, (2017). It might provide light on long-standing theoretical mysteries like the nature of singularities in black holes, spacetime quantization, and the unification of fundamental forces Marolf (2017)

Furthermore, the results of this study might be useful for detecting gravitational waves and for astrophysical observations Taveras (2008). Astronomers and astrophysicists could improve their methods of observation and understanding of gravitational lensing events by understanding the quantum gravitational effects on gravitational rainbows Magueijo & Smolin, (2003). This could result in the discovery of novel gravitational wave signatures or unusual astrophysical objects.

Additionally, this work has wider ramifications for research programs in quantum gravity and theoretical physics. It may contribute to the development of more thorough theories of quantum gravity and stimulate new experimental investigations of quantum gravitational effects in gravitational lensing scenarios by clarifying the implications of quantum gravity on observable phenomena such as gravitational rainbows.

In general, the goal of this work is to further the current conversation between observational astrophysics and quantum gravity theory, opening the door to a more profound comprehension of the underlying principles of gravity and spacetime.

1.3 Theoretical frameworks of quantum gravity

Quantum gravity is to bring general relativity and quantum mechanics into harmony, offering a cohesive framework for describing the fundamental forces of nature at their most basic. Numerous theoretical frameworks have been put out to tackle the difficulties presented by quantum gravity, each providing distinct viewpoints and understandings. Loop quantum gravity (LQG) is a well-known paradigm that depicts spacetime as a discrete network of connected loops or quantized spaces. Quantum gravitational effects can be expressed in LQG because discrete volume and area units are used to quantize the fabric of spacetime. According to Rovelli (2004), this method has significantly improved our knowledge of cosmology, black hole thermodynamics, and the early cosmos.

String theory is another theoretical framework that suggests that fundamental particles are extended one-dimensional strings vibrating at different frequencies rather than point-like entities. A possible path toward a consistent quantum theory of gravity is provided by string theory, which combines both general relativity and quantum mechanics. A foundation for examining the microscopic structure of spacetime and the genesis of gravitational phenomena is provided by string theory's complex mathematical structure and varied landscape of string configurations. Notwithstanding its difficulties, string theory has contributed significantly to our understanding of particle physics, quantum gravity, and the structure of spacetime Polchinski (1998). Among other things, these theoretical frameworks continue to influence how we think about quantum gravity and provide paths for more research and development to develop a comprehensive theory of quantum gravity.

1.4 Gravitational rainbows theory and predictions

According to the interesting gravitational rainbow idea, spectral bands that resemble rainbows are formed when light is dispersed by high gravitational fields. According to this hypothesis, light traveling through enormous objects like black holes and neutron stars experiences gravitational forces that bend and refract light, resulting in different wavelengths of light following different courses. Because of this, the light disperses into a spectrum, much like light does when it passes through a prism to form a rainbow. According to predictions, this phenomenon would happen close to black hole event horizons, where gravity is strongest. It may provide information about the properties of spacetime and gravity close to these cosmic objects Cunha et al. (2018).
Because of its implications for comprehending the underlying nature of gravity and the behavior of light in high gravitational conditions, the notion of gravitational rainbows has attracted significant interest in astrophysics and cosmology. Astronomers aim to test the predictions of alternative theories of gravity and general relativity and investigate the underlying features of spacetime by analyzing the spectral signatures of light emitted from sources close to black holes or other enormous objects. In addition, gravitational rainbow detections may yield important observational proof of the presence of black holes and other unusual astrophysical phenomena, illuminating some of the universe’s most mysterious objects Wei et al. (2018).

2. Materials and Methods

2.1 Research methods

Initially, we examine the fundamental formulas of quantum gravity, which seek to integrate general relativity with quantum mechanics to offer a more thorough comprehension of gravitational processes at the tiniest scales. We next expand these formulas to include the consequences of quantum gravity on light travel, especially in the vicinity of huge objects like neutron stars and black holes.

We use computational methods to modify equations of motion for light trajectories in the presence of quantum gravitational effects, to recreate gravitational rainbows. With the models, we can forecast the spectral patterns including gravitational rainbow formation that result from light interacting with strong gravitational fields. We explore the effects of quantum gravity on gravitational rainbows by adjusting factors like the mass and spin of the central object and the strength of quantum gravitational effects.

The comparison of theoretical predictions with observable data from astronomical observations, including gravitational lensing phenomena and measurements of the light spectra released by accretion disks around black holes. In addition to evaluating the practicality of our mathematical models, this comparative research sheds light on possible observable evidence of quantum gravitational effects on gravitational rainbows.

The method investigates the effects of quantum gravity on gravitational rainbows by fusing theoretical advances in quantum gravity with computational simulations and observational analyses. This advances our knowledge of the interactions among general relativity, quantum mechanics, and astrophysical phenomena.

3. Bibliographic review of quantum gravity’s effects on gravitational rainbows

To comprehend the implications of quantum gravity on gravitational rainbows, we must formulate the spacetime curvature mathematical statement. The Einstein field equations, which describe how matter and energy curve spacetime, are given to us by general relativity. These equations can be changed to include quantum effects in the setting of quantum gravity, which would cause them to deviate from classical predictions. We find the curvature of spacetime in the presence of quantum gravitational fields by solving the modified field equations Einstein (1915), and Hawking & Ellis (1973).

The Einstein field equations provide the curvature tensor $R_{\mu\nu}$, which describes the curvature of spacetime is

$$ R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{8\pi G}{c^4} T_{\mu\nu} $$

where $R_{\mu\nu}$ is the Ricci curvature tensor, $g_{\mu\nu}$ is the metric tensor, $R$ is the Ricci scalar, $T_{\mu\nu}$ is the stress-energy tensor, $G$ is the gravitational constant, and $c$ is the speed of light in a vacuum Einstein (1915) and Hawking & Ellis (1973).

The geodesic equation, which specifies the course that particles take in response to gravitational forces, controls particle motion in curved spacetime. Quantum gravitational effects can be considered by modifying the geodesic equation within the context of quantum gravity. We can forecast how particles, such as photons, diverge from their classical trajectories and contribute to the creation of gravitational rainbows by resolving the modified geodesic equation.

The geodesic equation in general relativity is given by

$$ \frac{d^2 x^\mu}{ds^2} + \Gamma^\mu_{\alpha\beta} \frac{dx^\alpha}{ds} \frac{dx^\beta}{ds} = 0 $$
where \( s \) is the affine parameter along the geodesic, \( x^\mu \) is the spacetime coordinates, and \( \Gamma^\mu_{\alpha\beta} \) is the second-kind Christoffel symbols, which represent the curvature of spacetime Misner et al. (1973) and Wald, (1984).

Changes to the geodesic equation in quantum gravity might result from extra quantum gravitational effects or from variations in the metric tensor. These adjustments may result in new terms being added to the geodesic equation and deviations from classical trajectories.

We can use approximations to make the equations regulating gravitational processes simpler in regimes with weak gravitational fields, such as those found near stars and planets. The linearized theory of gravity, which linearizes the field equations around a flat background spacetime, is one often used approximation. Although this approximation ignores nonlinear phenomena, it helps analyze gravitational rainbows in realistic astrophysical settings and offers insightful information about the dynamics of gravitational fields.

In the weak-field limit, the linearized field equations are provided by

\[
\mathbf{D}_\mu h_{\nu\mu} = -\frac{16\pi G}{c^4} T_{\nu\mu}
\]

where \( G \) is the gravitational constant, \( c \) is the speed of light in vacuum, \( T_{\nu\mu} \) is the stress-energy tensor, and \( h_{\mu\nu} \) is the perturbation of the metric tensor Weinberg (1972) and Carlip (2011).

The Newtonian potential \( \Phi \), which fulfills the Poisson equation, is one of the important solutions in the weak-field limit:

\[
\Delta^2 \Phi = 4\pi G \rho
\]

where \( \rho \) is the mass density.

We can investigate the propagation of gravitational waves and the bending of light rays in weak gravitational environments according to the linearized theory of gravity. We may examine the production of gravitational rainbows and compare the results with observations by solving the linearized field equations and applying the necessary boundary conditions Weinberg, (1972) and Carlip, (2011).

The deflection angle in gravitational physics describes how the gravitational field of a big object, like a star or black hole, causes light to deviate from its path as it approaches. The general theory of relativity's prediction of this event has been the focus of in-depth theoretical and observational research.

Mathematically, the geodesic equation in curved spacetime can be used to calculate the deflection angle \( \alpha \). Schwarzschild metric, which defines spacetime around a spherically symmetric mass, can be used to approximate the deflection angle for weak gravitational fields, as seen in the solar system Will, (2014) and Einstein, (1915). The deflection angle in this case is provided by

\[
\alpha = \frac{4GM}{c^2 b}
\]

where \( c \) is the speed of light in a vacuum, \( M \) is the mass of the deflecting object, \( G \) is the gravitational constant, and \( b \) is the impact parameter or the distance at which the light ray approaches the center of mass of the deflecting object Carroll, (2004).

Astrophysical phenomena like gravitational lensing and gravitational wave observations are significantly affected by the deflection angle estimate. It offers insightful information on spacetime's characteristics and the distribution of mass in the cosmos.

### 3.1 Computational simulations and modeling

In this work, modeling and computer simulations are essential tools for investigating how quantum gravity affects gravitational rainbows. We study the behavior of light near big objects under the impact of quantum gravitational effects using advanced computational techniques and mathematical models. We can anticipate the spectral patterns and distinctive properties of gravitational rainbows with high accuracy by incorporating concepts from general relativity and quantum mechanics into computational frameworks.

One method is to use computational algorithms to solve the modified equations of motion for light trajectories in
the presence of quantum gravitational forces. With the aid of these simulations, we can investigate the effects of quantum gravity on light bending and gravitational rainbow generation surrounding enormous objects, such as black holes and neutron stars. It can investigate the wide variety of events related to gravitational rainbows by adjusting parameters like the strength of quantum gravitational effects and the characteristics of the central object.

We can also produce synthetic data through computational simulations that can be compared to observational readings from astronomical observations. We may evaluate the precision and dependability of our computer models and obtain insights into possible observable signs of quantum gravitational effects on gravitational rainbows by comparing our theoretical predictions with observational data.

4. Results and Discussions
The results section looks into how quantum gravity affects gravitational rainbow production, providing insight into how quantum gravitational effects cause deviations from conventional predictions. We determine the amount to which quantum processes affect light's trajectory and contribute to the observed features of gravitational rainbow patterns by contrasting the outcomes of classical general relativity with those using quantum gravitational corrections. In addition, this section's analysis has consequences for how we comprehend the interaction between quantum mechanics and gravity. It sheds light on the underlying principles of spacetime and offers a framework for analyzing observational data from astrophysical phenomena such as gravitational lensing and light deflection.

Figure 1 shows the bending of light rays when approaching the massive objects. The deflection of light beams in the gravitational field of enormous objects, known as gravitational rainbows, is a phenomenon that depends on the angle at which the light rays are incident. To be more precise, the deflection angle tends to grow as the angle of incidence lowers, which corresponds to light rays approaching the large object more tangentially Einstein, (1915). On the other hand, when light beams strike at greater angles, the deflection angle decreases.

Figure 1. The bending of light rays around the massive object. Source: Author, 2024.

This result makes sense when considered in the context of gravitational lensing, an effect of the general theory of relativity where light beams passing close to big objects bend their courses. The gravitational field of a large object causes a light beam to deflect at an angle $\alpha$, which is inversely proportional to the impact parameter b. This angle indicates the closest approach of the light ray to the mass center of the huge object Will, (2014). This relationship can be stated mathematically as
The deflection angle $\alpha$ increases in proportion to a decrease in the angle of incidence due to a decrease in the impact parameter $b$. On the other hand, the impact parameter rises with greater angles of incidence, resulting in a smaller deflection angle Carroll, (2004).

Moreover, the mass of the huge object has an impact on the deflection angle. The mass $\alpha$ of the deflecting object is directly proportional to the deflection angle $\alpha$, as per Einstein's general theory of relativity Will, (2014).

To replicate quantum gravitational effects, we add a fictitious correction factor to the gravitational potential equation. The correction term is proportional to $\hbar/(r^2c)$, where $c$ is the speed of light and $\hbar$ is the reduced Planck constant. This word denotes a possible quantum effect-related alteration to the classical gravitational field.

The gravitational potential in Newtonian mechanics is shown in (Figure 2). In terms of physics, the outcome depicted in (Figure 2) is consistent with Newtonian gravity, which holds that a point mass's gravitational potential is infinite in all directions. The inverse square law states that the gravitational potential reduces with increasing distance from the point mass, but it never completely approaches zero Walker, (2013), Taylor & Wheeler, (1992), and Thornton & Marion, (2004). Therefore, gravitational potential values are not zero even at great distances.

Figure 2. The gravitational potential according to Newton’s mechanics. Source: Author, 2024.

Newton's equations of motion and universal gravitation, which define how masses attract one another with a force that depends on their masses and the distance between them, are consistent with this behavior Halliday & Walker, (2013), Taylor & Wheeler, (1992) and Thornton & Marion, (2004). Newton's equations of motion state that the gravitational potential, when applied to a point mass, is constant across space but diminishes with increasing distance from the mass.

A cornerstone of gravitational physics and classical mechanics is the physical interpretation of gravitational fields directed toward the center of mass. The inverse square law of gravity, which states that the gravitational force between two objects is inversely proportional to the square of their distance apart and directly proportional to the product of their masses, is responsible for this behavior as shown in (Figure 3).
A cornerstone of gravitational physics and classical mechanics is the physical interpretation of gravitational fields directed toward the center of mass. The inverse square law of gravity, which states that the gravitational force between two objects is inversely proportional to the square of their distance apart and directly proportional to the product of their masses, is responsible for this behavior.

The classical predictions of gravitational fields are likely to be modified by quantum gravitational phenomena, especially at very small scales or high energies. A quantum correction term that modifies the behavior of gravity on those scales could be suggested by the outward, diminishing gravitational potential dispersion.

Similar to how rainbows develop from the refraction of light by water droplets, gravitational rainbows are created when light is bent by the gravitational field of huge objects. The outward dispersion of gravitational potential in the framework of quantum gravity could point to a more expansive and diffuse gravitational field surrounding the big item.

The paths taken by light rays as they travel through the gravitational field may be impacted by the altered gravitational potential. The quantum corrections could cause a more gradual divergence of light pathways, similar to a gravitational rainbow, rather than the acute bending of light that classical gravity predicts.

Though theoretical, these interpretations can direct theoretical research and experimental experiments that explore the consequences of quantum gravity. Light-bending observations around enormous objects, such as stars or black holes, may show variations from classical expectations and support the existence of quantum gravitational phenomena.

Different theoretical approaches to quantum gravity are proposed by frameworks like string theory, loop quantum gravity, or emergent gravity, which may provide insights into the behavior of gravitational forces at small scales. It will need additional theoretical and observational research to fully comprehend the implications of these frameworks for phenomena such as gravitational rainbows.

Overall, a modification to classical gravity that may affect the production of gravitational rainbows is suggested by understanding the outward spread of gravitational potential in the context of quantum gravitational effects. Validating these interpretations and revealing the true nature of quantum gravity will require more theoretical work and experimental research.

This localization of the linear fields is shown in (Figure 4). The result shows that the mass distribution is positioned close to the center of the coordinate system, where the gravitational perturbations, indicated by $h_{xx}$ and $h_{yy}$, are strongest. According to the linearized theory of gravity, gravitational influences are strongest close to huge objects and are weaker quickly as one gets farther away from the source. As a result, $h_{xx}$ and $h_{yy}$ are concentrated close to the origin, which is where the mass distribution is thought to be.
When compared to the gravitational perturbations in the x and y directions, the z-direction's perturbations appear to be either negligible or much weaker when no display is observed for $h_{zz}$. This could be caused by many things, including the coordinate system selected or the mass distribution's presumed symmetry. Asymmetrical perturbations can occur when some directions show higher gravitational effects than others.

Overall, as expected by the linearized theory of gravity, these findings emphasize the concentrated character of gravitational disturbances close to huge objects. The perturbation components' unique localization and asymmetry can reveal important details about the mass distribution and spacetime geometry close to the source. Understanding the gravitational effects in three dimensions may require additional research and model improvement.

The light appears to be traveling along the x-axis seen in (Figure 5) at a constant speed if the pathway between the x-coordinate and affine parameter is a straight line. This might indicate a situation in which there are no external factors influencing the light's velocity and the gravitational field is weak or uniform.

The geodesic, or shortest path between two places in curved spacetime, is the path that light (or any other free-falling particle) travels along in the framework of general relativity. A straight line may be seen in the geodesic trajectory if the spacetime is locally flat or almost flat.
by the local spacetime geometry.

Gravity has an impact even when geodesic motion is homogeneous along the path chosen by spacetime curvature. The curvature of spacetime and the consequent geodesic motion are caused by gravity alone. Due to the force of gravity, objects in free fall, including light, adhere to geodesics exactly.

Overall, a straightforward and predictable motion of light along the x-axis is shown by a straight-line pathway between the affine parameters and the x-coordinate. To properly understand the importance of such a discovery in the particular scenario under study, more investigation and attention to the physical context such as the type of gravitational field or the existence of additional forces are required.

Gravitational rainbow dynamics and appearance are significantly shaped by time dilation, an effect of Einstein's theory of relativity Einstein, (1916) and Hartle, (2003). When compared to observers in weaker gravitational fields, time appears to move more slowly in areas of powerful gravitational fields, such as those surrounding big objects. Rainbow events' genesis, evolution, and persistence are impacted by the temporal aberrations caused by this phenomenon. Because gravitational time dilation affects how quickly things happen, observers in areas with higher gravitational potentials would see rainbow occurrences happening more slowly than those in areas with lesser gravitational influences Carroll, (2004) and Wald, (1984). As a result, in areas with higher gravity, the length of rainbow events like light refraction and dispersion via water droplets may be extended, changing the gravitational rainbow's apparent look and dynamics.

The gravitational redshift phenomena can be used to formulate mathematically the effects of time dilation on rainbow gravitation. The change in light's frequency (and hence wavelength) when it passes through a gravitational field is known as the gravitational redshift. It is given by

\[
\frac{\Delta \lambda}{\lambda} = \frac{\Delta t}{t} = \frac{GM}{c^2 r}
\]

where \(G\) is the gravitational constant, \(M\) is the mass of the gravitating object, \(c\) is the speed of light, \(r\) is the distance from the gravitational field's center, \(\Delta \lambda\) is the change in wavelength, \(\lambda\) is the original wavelength, and \(\Delta t\) is the change in time. The phrase measures the extent of wavelength shift, and consequently, redshift, that light experiences as a result of the gravitational force. This, in turn, represents the effect of time dilation on the characteristics of gravitational rainbows that are observed. A thorough grasp of the dynamics of gravitational rainbow events within the framework of relativistic effects can be obtained by incorporating these factors into the analysis.

According to Einstein's general theory of relativity, time dilation is the phenomenon where an observer's perception of time varies based on their motion and the gravitational field they are in. Time seems to move more slowly in the vicinity of huge objects than it does in areas where gravitational fields are weaker. The following formula can be used to determine the time dilation factor:

\[
t_d = \sqrt{1 - \frac{2GM}{c^2 r}}
\]

The gravitational field, which modifies both the frequency and the passage of time, is what causes this redshift. The gravitational redshift formula can be used to express the relationship between time dilation and redshift is

\[
1 + z = \frac{1}{\sqrt{1 - \frac{GM}{c^2 r}}}
\]

The redshift values derived from the modified equation of motion provide interesting insights into the effects of gravity on light propagation, especially when taking realistic masses of astronomical objects (in terms of solar masses) shown in (Figure 6 (a)). The redshift values' order of magnitude, which is usually about 1e-2, indicate how much the gravitational field of big objects influences the wavelengths of photons that are traveling through space.

According to general relativity, gravitational redshift is the result of huge objects distorting spacetime, which
causes light to shift in frequency as it moves away from gravitational sources shown in (Figure 6 (b)). The gravitational object's mass and distance from the subject determine how much of a shift there will be. Light's behavior near huge objects can be understood from many angles thanks to the modified equation of motion derived from quantum gravitational theories, yet classical general relativity still gives a strong framework.

Figure 6. a) The quantum gravitational impacts on the redshift when the light approaches the heavy mass and b) the impacts in redshift based on the Einstein equation. Source: Author, 2024.

The observed correspondences between the redshift values derived from the quantum and classical gravitational viewpoints imply that the altered equation of motion adequately describes fundamental features of gravitational interactions, albeit in a distinct theoretical context shown in (Figure 6). This agreement with classical results highlights how quantum gravity theories can offer further insights into known processes.

To completely comprehend the effects of quantum gravity on gravitational redshift and to resolve any differences between quantum and classical predictions, more theoretical and experimental research is necessary. Researchers can learn more about the fundamentals of gravity and how it affects light propagation in the cosmos by combining ideas from both classical and quantum gravitational theories.

Figure 7. The difference in the redshift between quantum gravity vs classical gravity. Source: Author, 2024.
As Figure 7 illustrates, the redshift values obtained from the perspectives of quantum gravity and classical gravity differ, providing fascinating new information on the behavior of light close to huge celestial objects. Classical gravity seems to predominate at lower masses, where the differences between the two views are minimal Amelino-Camelia et al. (2013); Ashtekar & Lewandowski (2004). This finding is in line with the well-established theory of general relativity, which emphasizes the importance of classical gravitational effects in explaining how light behaves when it is near relatively small masses Barceló et al. (2002) and Thiemann, (2007).

The distinctions between quantum gravity redshift and classical gravity become more noticeable as the mass of the gravitational object rises. This implies that the observed redshift values are more significantly shaped by quantum gravitational effects at larger masses. This phenomenon is especially noteworthy in astrophysical scenarios where quantum gravitational effects are anticipated to be important, such as those involving huge celestial objects like galaxies, black holes, and neutron stars.

This view is consistent with the increasing amount of research that examines how classical, and quantum gravitational theories interact to explain gravitational occurrences Rovelli, (2004). In light of recent research, it is critical to take into account both classical and quantum viewpoints to fully comprehend how light and other physical phenomena behave in gravitational fields. Through the use of quantum gravity theories, scientists hope to improve our comprehension of basic gravitational processes and tackle longstanding issues in cosmology and astrophysics.

4. Conclusions

The following conclusions can be made in light of the data gathered from the examination of numerous phenomena about light propagation and gravitational effects. Light is traveling along the x-axis at a constant speed when a straight-line trajectory is observed between the affine parameters and the x-coordinate. This is consistent with the basic idea of light propagation, which states that photons move at a fixed speed and is commonly expressed as the speed of light in a vacuum.

The paths taken by light rays as they travel through the gravitational field are greatly impacted by the changing gravitational potential. The research shows that the gravitational potential expands outward, decreasing towards zero outward and reaching magnitudes as high as $1.0 \times 10^{11}$ outward. This finding emphasizes how light behaves in gravitational fields due to quantum gravitational phenomena.

The mass distribution is found close to the coordinate system's center, where the distribution of gravitational perturbations, denoted by $h_{xx}$ and $h_{yy}$, is highest. Furthermore, the fact that $h_{zz} = 0$ implies that gravitational disturbances in the z-direction are either very small or much less powerful than those in the x and y directions.

Based on a drop in the impact parameter $b$, the study shows that the deflection angle $\alpha$ grows proportionally to a decrease in the angle of incidence. Furthermore, the deflecting object's mass directly affects the deflection angle $\alpha$, suggesting a proportionate relationship between the object's mass and the amount of deflection that light rays encounter.

The findings shed important light on how light behaves in gravitational fields, how changing gravitational potentials affect deflection angles, and how the mass of deflecting objects affects them. These discoveries advance our knowledge of gravitational phenomena and have ramifications in many astrophysical and cosmological domains.

In theoretical physics, quantum gravity rainbows are a theoretical notion suggesting quantum gravity's effects may modify particle dispersion relations, causing an energy-momentum relationship distortion similar to light diffractive effects through a prism. If these changes pass, they would appear as energy-dependent spacetime structures, which would have fascinating ramifications for our comprehension of basic physics and spacetime. It is crucial to remember that rainbows resulting from quantum gravity are still theoretical and speculative, needing empirical confirmation through testing in experiments or additional theoretical advancement. As such, their eventual significance and validity within the context of fundamental physics remain unclear, even if they present interesting directions for investigation.

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